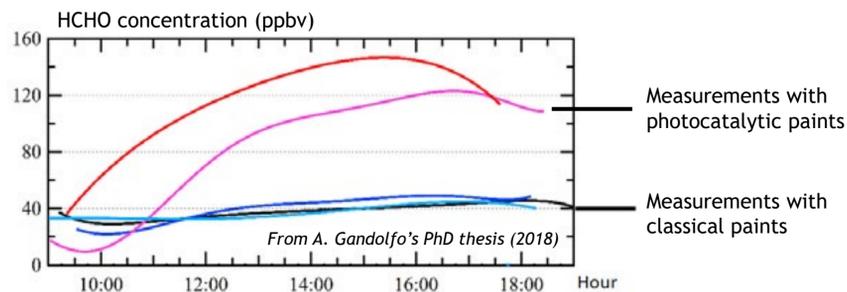


1. Motivation

Context : Development of paints containing TiO₂ nanoparticles (NPs) as a means to improve indoor air quality (IAQ). The photo-activated TiO₂ NPs produce OH radicals that can degrade volatile organic compounds (VOCs).

Problematic : Measurements performed in a room whose walls were covered by such paints, revealed a completely opposite effect, with a strong increase of pollution level.

Aim : Developing a numerical model allowing to simulate indoor concentrations to understand and assess the effect of these photocatalytic paints on IAQ.



2. Presentation of the H²I model

The H²I (Homogeneous Heterogeneous Indoor) model is a **two-box model** allowing to differentiate the volume illuminated by the direct light of the sun (denoted L), and the volume illuminated by indirect light (denoted S). The time evolution of the concentrations in the boxes is defined as :

$$\frac{dC_i^L}{dt} = \underbrace{k_{AER}(fC_i^{Out} - C_i^L)}_{\text{Exchanges between the room and its outside}} - \underbrace{k_{DEP,i}^L C_i^L}_{\text{Deposition}} + \underbrace{k_{BOX}^L (-C_i^L + C_i^S)}_{\text{Exchanges between the boxes}} + \underbrace{\frac{Q_{room,i}}{V_{room}} + \frac{E_{paint,i}^L S_{paint,i}^L}{V_{box}^L}}_{\text{Room and paints emissions}} + \underbrace{\sum_q \frac{R_{iq}^j}{V_{box}^L}}_{\text{Chemical reactivity}}$$

$$\frac{dC_i^S}{dt} = \underbrace{k_{AER}(fC_i^{Out} - C_i^S)}_{\text{Exchanges between the room and its outside}} - \underbrace{k_{DEP,i}^S C_i^S}_{\text{Deposition}} + \underbrace{k_{BOX}^S (C_i^L - C_i^S)}_{\text{Exchanges between the boxes}} + \underbrace{\frac{Q_{room,i}}{V_{room}} + \frac{E_{paint,i}^S S_{paint,i}^S}{V_{box}^S}}_{\text{Room and paints emissions}} + \underbrace{\sum_q \frac{R_{iq}^j}{V_{box}^S}}_{\text{Chemical reactivity}}$$

- t : time [s]
- C_i^{L,S} : concentration of species i in box L,S [μg.m⁻³]
- C_i^{Out} : outdoor concentration of species i [μg.m⁻³]
- f : building filtration factor [-]
- k_{AER} : air exchange rate between the room and its outside [s⁻¹]
- k_{DEP,i} : deposition rate of species i [s⁻¹]
- k_{BOX} : air exchange rate between the boxes [s⁻¹]
- V_{room} : total volume of the room [m³]
- V_{box}^{L,S} : volume of box L,S [m³]
- Q_{room,i} : room emission rate of species i [μg.s⁻¹]
- S_{paint,i}^{L,S} : surface of paint in box L,S [m²]
- E_{paint,i}^{L,S} : paint emission rate of species i in box L,S [μg.m⁻².s⁻¹]
- R_{iq} : mass reaction rate between species i and species q [μg.s⁻¹]

3. Heterogeneous reactivity

Organic and inorganic species can sorb on surfaces at a rate k_{DEP} defined as :

$$\frac{1}{k_{DEP,i}^j} = \frac{1}{k_{tran,i}^j} + \frac{1}{k_{react,i}^j}$$

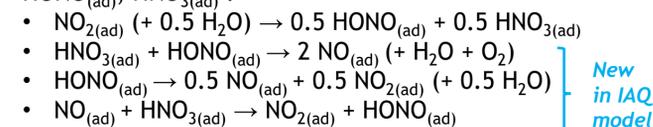
- v_{trd,i} : deposition velocity of species i [m.s⁻¹] (depends on the speed of air mixing)
- γ_i : uptake coefficient of species i [-]
- ω_i : thermal velocity of species i [m.s⁻¹]
- j : box indicator (L or S)
- S_{box}^j : box solid surface [m²]

$$k_{tran,i}^j = v_{trd,i} \frac{S_{box}^j}{V_{box}^j} \quad k_{react,i}^j = \frac{\gamma_i \omega_i S_{box}^j}{4 V_{box}^j}$$

Transport to surfaces

Efficiency of collisions with surfaces

Once sorbed, the organic and some inorganic species like ozone are assumed to stay adsorbed or to be degraded by the photocatalyst. The NO_y compounds (NO, NO₂, HONO) have the possibility to react thanks to the introduction of sorbed compounds NO_(ad), NO_{2(ad)}, HONO_(ad), HNO_{3(ad)} :



Finally, the NO_y compounds can desorb at a rate k_{i,(ad)} = k'_{i,(ad)} n_{H₂O} where n_{H₂O} is the number of water molecules computed from absolute humidity.

4. Input data and model parameters

Input data :

- Room temperature and relative humidity
- Evolution of the volumes and surfaces of the boxes
- Photolysis constants for both boxes
- VOCs, NO, NO₂ and O₃ outdoor concentrations
- VOCs, NO_y and O₃ initial indoor concentrations
- NO₂ uptake coefficient + parameterization with temperature and humidity
- Ventilation rate k_{AER}

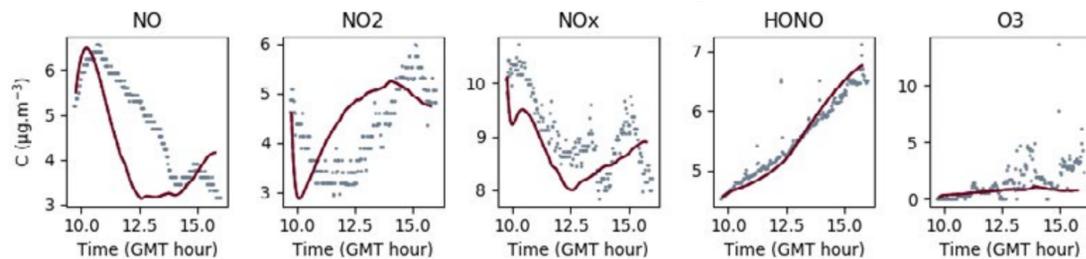
Model parameters :

- Building filtration factor and average speed of air in the room
- NO, HONO and O₃ uptake coefficients γ_i
- NO, NO₂ and HONO evaporation constants k'_{i,(ad)}
- Stoichiometry of the NO₂ heterogeneous hydrolysis : NO_{2(ad)} → B_{HNO₃} HNO_{3(ad)} + B_{HONO} HONO_(ad)
- Kinetic rates of the surface reactions

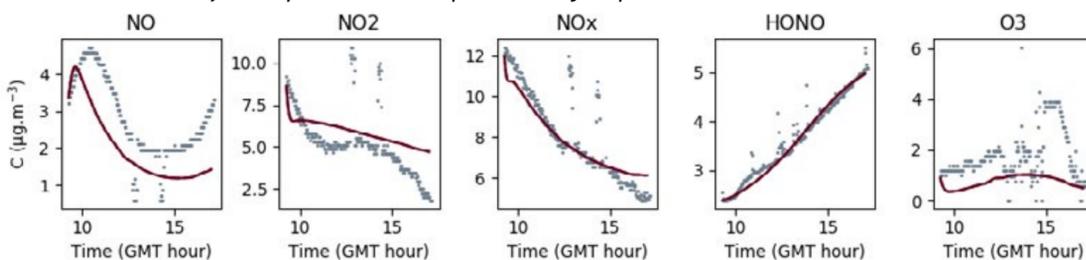
5. Simulations of the experiments

The simulations are performed by constraining the organic compounds to their measured values. The model parameters are adapted to achieve the least error as possible between data (grey curve) and model (red curve), for the four measured inorganic species (NO, NO₂, HONO, O₃). The model parameters share the same values for the three simulated experiments, apart from the desorption constants.

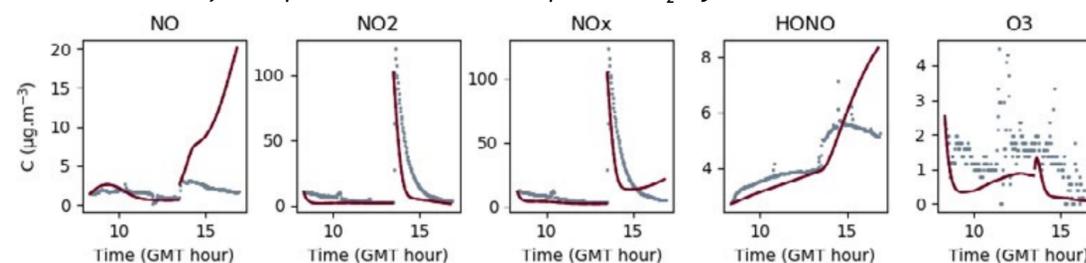
Simulation of an experiment with classical paint (no TiO₂ NPs) :



Simulation of an experiment with photocatalytic paint :



Simulation of an experiment with classical paint + NO₂ injection :



Satisfying results are achieved for the four inorganic compounds, unless in the experiment with NO₂ injection, which calls for a more complex parameterization of desorption. We can note that the type of paint does not influence the modelled/measured inorganic concentrations.

6. Conclusion

The H²I model has been developed to simulate the chemistry of inorganic compounds in indoor environments. It can now be further developed to simulate the organic compounds concentrations using the paint emission rates determined in reactor experiments. In the future, such development should allow to assess the depollution efficiency of other NPs-bearing paint characterized experimentally, without the necessity to perform an indoor campaign.

Reference : Eve-Agnès Fiorentino, Henri Wortham, and Karine Sartelet. Combining homogeneous and heterogeneous chemistry to model inorganic compounds concentrations in indoor environments: the H²I model (v1.0). Geoscientific Model Development Discussions, 2020:1-58, 2020. URL: <https://gmd.copernicus.org/preprints/gmd-2020-300/>